

# Basic and Advanced Database Courses

**Srdjan Škrbić**

*Faculty of Science, University of Novi Sad  
Trg Dositeja Obradovića 4, 21000 Novi Sad, Serbia  
shkrba@uns.ac.rs  
<http://www.is.pmf.uns.ac.rs/skrbics>*

At the beginning of the course, we explore some basic database concepts and adopt terminology. We give an overview of the most important data models. First we give brief remarks on historical network and hierarchical data models, and then we continue to investigate entity-relationship and relational data model. Only most important facts about entity-relationship model, together with some examples will be covered. The relational data model will be presented in much more detail, but we concentrate on exploring possibilities for its practical usage. Important remarks about theoretical background of the relational model are covered later in the text. We continue with the most important constructions of the Structured Query Language.

In the advanced level course, we concentrate on the theoretical background of the relational model, explore it in some detail, and explain implications these concepts make to the usage of the relational model in practice. Among other topics, we explore functional dependencies in detail. Next, we give some pointers on update anomalies and the need to introduce normal (canonical) forms to relational database theory. We describe normal forms from first to third, including the Boyce-Codd normal form that belongs somewhere between the third and the fourth. We also give pointers about other normal forms. At the end we introduce two algorithms for relational database normalization - decomposition and synthesis.

## 1. Introduction

Databases today are essential to every business. Whenever you visit a major Web site Google, Yahoo!, Amazon.com, or thousands of smaller sites that provide information there is a database behind the scenes serving up the information you request. Corporations maintain all their important records in databases. Databases are likewise found at the core of many scientific investigations. They represent the data gathered by astronomers, by investigators of the human genome, and by biochemists exploring properties of proteins, among many other scientific activities. The power of databases comes from a body of knowledge and technology that has developed over several decades and is embodied in specialized software called a database management system, or DBMS. A DBMS is a powerful tool for creating and managing large amounts of data efficiently and allowing it to persist over long periods of time, safely. These systems are among the most complex types of software available.

In essence a database is nothing more than a collection of information that exists over a long period of time. The term database also refers to a collection of data that is managed by a DBMS. The DBMS is expected to allow users to:

- create new databases and specify their schemas,
- query the data and modify the data,
- support the storage of very large amounts of data,

- enable durability, the recovery of the database in the face of failures and
- control access to data from many users at once, without allowing unexpected interactions among users and without actions on the data to be performed partially but not completely.

The early DBMS's required the programmer to visualize data much as it was stored. These database systems used several different data models for describing the structure of the information in a database. Two most important models were "hierarchical" or tree-based model and the graph-based "network" model. A problem with these early models and systems was that they did not support high-level query languages. That is why there was considerable effort needed to write such programs, even for very simple queries.

Following a famous paper written by Codd [3] in 1970, database systems changed significantly. Codd proposed that database systems should present the user with a view of data organized as tables called relations. Behind the scenes, there might be a complex data structure that allowed rapid response to a variety of queries. But, unlike the programmers for earlier database systems, the programmer of a relational system would not be concerned with the storage structure. Queries could be expressed in a very high-level language, which greatly increased the efficiency of database programmers.

By 1990, relational database systems were the norm. Yet the database field continues to evolve, and new issues and approaches to the management of data surface regularly. Object-oriented features have infiltrated the relational model. Some of the largest databases are organized rather differently from those using relational methodology.

## 1.1. Overview of a Database Management System

In Fig. 1 we see an outline of a complete DBMS. Single boxes represent system components, while double boxes represent in-memory data structures. The solid lines indicate control and data flow, while dashed lines indicate data flow only. Since the diagram is complicated, we shall consider the details in several stages. First, at the top, we suggest that there are two distinct sources of commands to the DBMS:

1. Conventional users and application programs that ask for data or modify data.
2. A database administrator: a person or persons responsible for the structure or schema of the database.

### 1.1.1. Query Processing

The second kind of command is the simpler to process, and we show its trail beginning at the upper right side of Fig. 1. For example, the database administrator, or DBA, for a university registrar's database might decide that there should be a table or relation with columns for a student, a course the student has taken, and a grade for that student in that course. The DBA might also decide that the only allowable grades are A, B, C, D, and F. This structure and constraint information is all part of the schema of the database. It is shown in Fig. 1 as entered by the DBA, who needs special authority to execute schema-altering commands, since these can have profound effects on the database. These schema-altering data-definition language (DDL) commands are parsed by a DDL processor and passed to the execution engine, which then goes through the index/file/record manager to alter the meta data, that is, the schema information for the database.

The great majority of interactions with the DBMS follow the path on the left side of Fig. 1. A user or an application program initiates some action, using the data-manipulation language (DML). This command does not affect the schema of the database, but may affect the content of the database or will extract data from the database.

The query is parsed and optimized by a query compiler. The resulting query plan, or sequence of actions the DBMS will perform to answer the query, is passed to the execution engine. The execution engine issues a sequence of requests for small pieces of data, typically records or tuples of a relation, to a resource manager that knows about data files (holding relations), the format and size of records in those files, and index files, which help find elements of data files quickly.

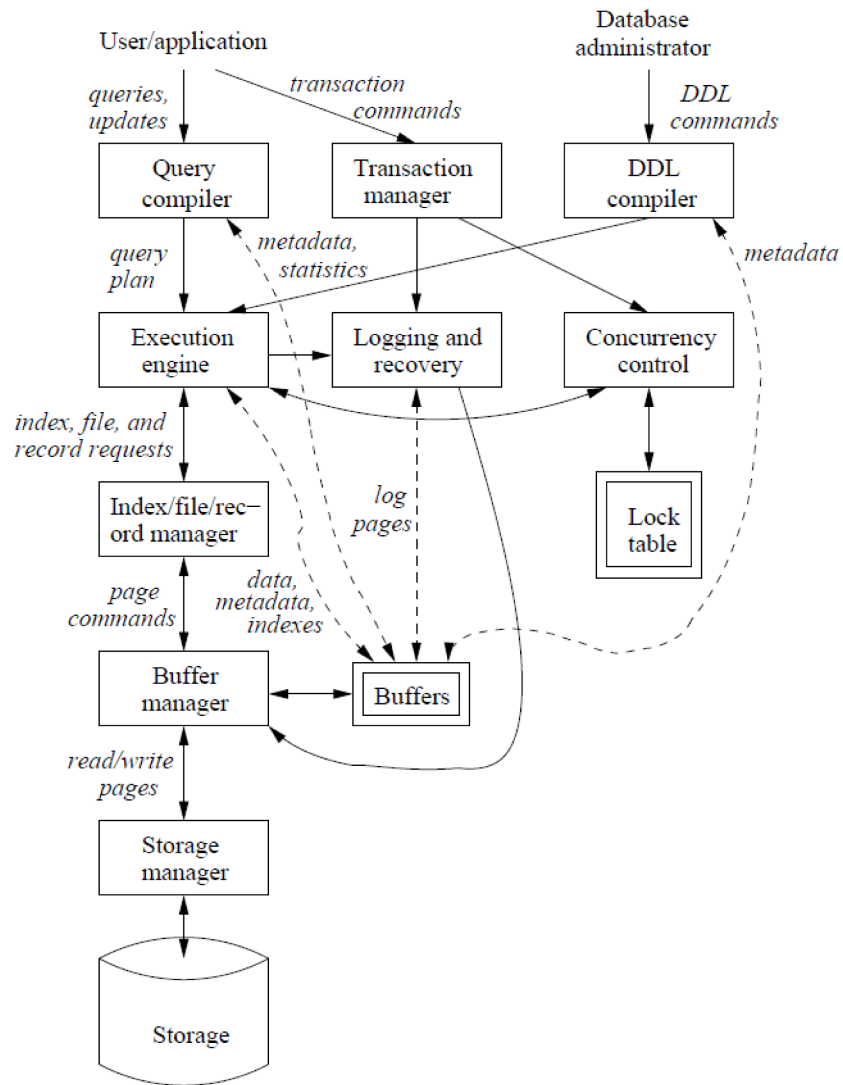


Figure 1: DBMS components.

The requests for data are passed to the buffer manager. The buffer manager's task is to bring appropriate portions of the data from secondary storage (disk) where it is kept permanently, to the main-memory buffers. Normally, the page or "disk block" is the unit of transfer between buffers and disk.

The buffer manager communicates with a storage manager to get data from disk. The storage manager might involve operating-system commands, but more typically, the DBMS issues commands directly to the disk controller.

Queries and other DML actions are grouped into transactions, which are units that must be executed atomically and in isolation from one another. Any query or modification action can be a transaction by itself. In addition, the execution of transactions must be durable, meaning that the effect of any completed transaction must be preserved even if the system fails in some way right after completion of the transaction.

### 1.1.2. Storage and Buffer Management

The data of a database normally resides in secondary storage - a magnetic disk, for example. However, to perform any useful operation on data, that data must be in main memory. It is the job of the storage manager to control the placement of data on disk and its movement between disk and main memory. For efficiency purposes, DBMS's normally control storage on the disk directly, at least under some circumstances. The storage manager keeps track of the location of files on the disk and obtains the block or blocks containing a file on request from the buffer manager.

The buffer manager is responsible for partitioning the available main memory into buffers, which are page-sized regions into which disk blocks can be transferred. Thus, all DBMS components that need information from the disk will interact with the buffers and the buffer manager, either directly or through the execution engine. The kinds of information that various components may need include: data, meta data, log records, statistics, indexes, etc.

### 1.1.3. Transaction Processing

It is normal to group one or more database operations into a transaction, which is a unit of work that must be executed atomically and in apparent isolation from other transactions. In addition, a DBMS offers the guarantee of durability: that the work of a completed transaction will never be lost. The transaction manager therefore accepts transaction commands from an application, which tell the transaction manager when transactions begin and end, as well as information about the expectations of the application.

The transaction processor performs the following tasks:

1. Logging: In order to assure durability, every change in the database is logged separately on disk.
2. Concurrency control: The concurrency-control manager must assure that the individual actions of multiple transactions are executed in such an order that the net effect is the same as if the transactions had in fact executed in their entirety, one-at-a-time.
3. Deadlock resolution: As transactions compete for resources through the locks that the scheduler grants, they can get into a situation where none can proceed because each needs something another transaction has. The transaction manager has the responsibility to intervene and cancel ("rollback" or "abort") one or more transactions to let the others proceed.

Properly implemented transactions are commonly said to meet the "ACID test", where:

- "A" stands for "atomicity," the all-or-nothing execution of transactions.
- "C," stands for "consistency." That is, all databases have consistency constraints, or expectations about relationships among data elements.
- "I" stands for "isolation," the fact that each transaction must appear to be executed as if no other transaction is executing at the same time.

- "D" stands for "durability," the condition that the effect on the database of a transaction must never be lost, once the transaction has completed.

#### 1.1.4. The Query Processor

The portion of the DBMS that most affects the performance that the user sees is the query processor. In Fig. 1 the query processor is represented by two components - the query compiler and the execution engine.

The query compiler, which translates the query into an internal form called a query plan. The latter is a sequence of operations to be performed on the data. The query compiler consists of three major units:

1. A query parser, which builds a tree structure from the textual form of the query.
2. A query pre processor, which performs semantic checks on the query and performing some tree transformations to turn the parse tree into a tree of algebraic operators representing the initial query plan.
3. A query optimizer, which transforms the initial query plan into the best available sequence of operations on the actual data.

The execution engine, which has the responsibility for executing each of the steps in the chosen query plan. The execution engine interacts with most of the other components of the DBMS, either directly or through the buffers. It must get the data from the database into buffers in order to manipulate that data. It needs to interact with the scheduler to avoid accessing data that is locked, and with the log manager to make sure that all database changes are properly logged.

## 2. Data models

The notion of a "data model" is one of the most fundamental in the study of database systems. In this brief summary of the concept, we define some basic terminology and mention the most important data models.

A data model is a notation for describing data or information. The description generally consists of three parts:

1. Structure of the data. The data structures used to implement data in the computer are sometimes referred to as a physical data model. In the database world, data models are at a somewhat higher level than data structures, and are sometimes referred to as a conceptual model to emphasize the difference in level.
2. Operations on the data. In database data models, there is usually a limited set of operations that can be performed. We are generally allowed to perform a limited set of queries (operations that retrieve information) and modifications (operations that change the database). By limiting operations, it is possible for programmers to describe database operations at a very high level, yet have the database management system implement the operations efficiently.
3. Constraints on the data. Database data models usually have a way to describe limitations on what the data can be. These constraints can range from the simple (e.g., "a day of the week is an integer between 1 and 7" or "a movie has at most one title") to some very complex forms of limitations.

Here we give an overview of the two most important data models - the entity-relationship and the relational model.

### 2.1. Entity-relationship model

Entity-relationship diagrams were first proposed as a means of quickly obtaining, with minimum effort, a good sense of the structure of a database [14]. They are used to plan and design a database and to model a system's data.

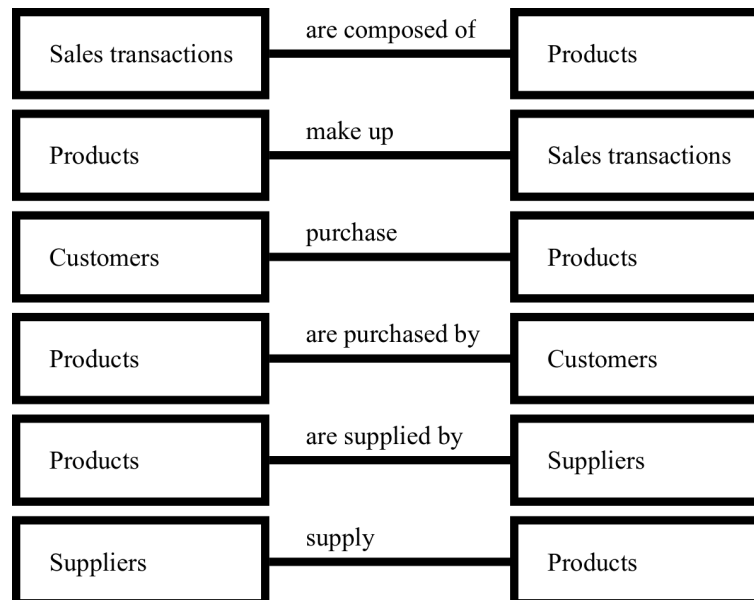


Figure 2: A relationship between two entities is shown by drawing a line between them.

An entity-relationship diagram is an excellent tool for planning and designing a database, particularly when used in conjunction with data normalization. The entity-relationship model starts with the entities, data normalization starts with the attributes, and the two tools tend to verify each other. The entity-relationship model's entities, attributes, and relationships map smoothly to a physical database.

During the systems analysis phase, an entity-relationship diagram gives the analyst a clear, high-level view of the data. Used in conjunction with data flow diagrams, an entity-relationship model gives the analyst an alternative logical view of the system. If a great deal is known about the data but not much about the processes, an entity-relationship diagram is an excellent starting point for modeling the system.

An entity-relationship model is data driven. The model implies processes but does not clarify the processes. Non-technical people find entity-relationship models difficult to understand and the nature of a relationship (one, many) confusing, and numerous notational variations sometimes make it difficult for even an experienced person to quickly grasp a particular diagram.

Before creating an entity-relationship diagram, the analyst must have at least a preliminary sense of the system's logical entities, attributes, and data structures. The necessary information is obtained during the information gathering and problem definition stage. Entity-relationship diagrams are important tools in the structured requirements methodology and in database design. They are often used in conjunction with data flow diagrams and data normalization.

### 2.1.1. Concepts

Entity-relationship diagrams are used to plan and design a database and to model a system's data. An entity is an object (a person, group, place, thing, or activity) about which data are stored. A relationship links two entities and is shown by drawing a line between them (Fig. 2).

Logically, a relationship can be stated in the form of a sentence with a verb linking the two entities. For example: sales transactions are composed of products, or products make up sales transactions.

The act of creating such sentences is a good test of the relationship's validity. In cases where the relationship is unclear, the sentence might be written alongside the relationship line as shown in Fig. 2. A given relationship can be mandatory (shown by a solid line) or optional (a broken line).

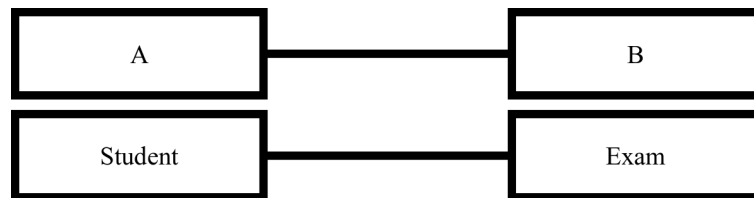


Figure 3: One-to-one relationship.

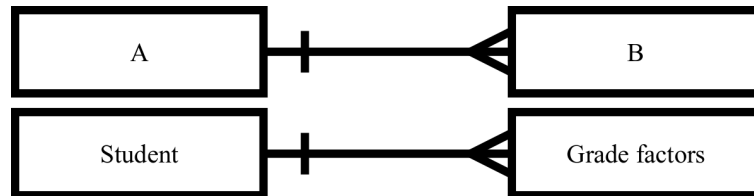


Figure 4: One-to-many relationship.

### 2.1.2. Relationships

For a variety of reasons, some relationships are more stable and easier to maintain than others. (A detailed discussion of the underlying database theory is beyond the scope of this course.) Cardinality, a measure of the related entities' relative number of occurrences, is an important predictor of the strength of the relationship.

In a one-to-one relationship, each occurrence of entity A is associated with one and only one occurrence of entity B, and each occurrence of entity B is associated with one and only one occurrence of entity A (Fig. 3).

For example, imagine that an instructor maintains examination grades for each student in his or her class. There are two entities in this example: Students and Exams. For each Student there is one and only one Exam, and for each Exam there is one and only one Student.

Graphically, a one-to-one relationship is described by drawing short crossing lines at both ends of the line that links the two entities (Fig. 3). However, some practitioners simply show the relationship line with no embellishment, and other symbols are used as well.

In a one-to-many relationship, each occurrence of entity A is associated with one or more occurrences of entity B, but each occurrence of entity B is associated with only one occurrence of entity A (Fig. 4).

For example, a student's grade in most courses is based on numerous grade factors (such as exams, papers, and projects). A given Student has several different Grade factors, but a given Grade factor is associated with one and only one Student.

Graphically, a one-to-many relationship is shown by drawing a short crossing line (or no extra marking) at the 'one-end' and a small triangle (sometimes called a crow's foot) at the 'many-end' of the relationship line (Fig. 4). Some practitioners use other symbols, however.

In a many-to-many relationship, each occurrence of entity A is associated with one or more occurrences of entity B, and each occurrence of entity B is associated with one or more occurrences of entity A (Fig. 5). For example, a student's end-of-term Grade report can list several Courses, and a given Course can appear on many students' Grade reports.

Graphically, a many-to-many relationship is shown by drawing a crow's foot at both ends of the relationship line (Fig. 5). Again, some practitioners use other symbols.

Here we focus on one-to-one, one-to-many, and many-to-many relationships, other types of relationships are possible. Sometimes entities are mutually exclusive, with A linked to either B or C, but not both. In a mutually inclusive relationship, if A is linked to B it must also be linked to C. Zero cardinality implies that an occurrence of

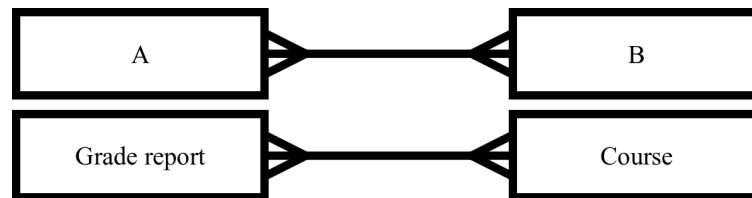


Figure 5: Many-to-many relationship.

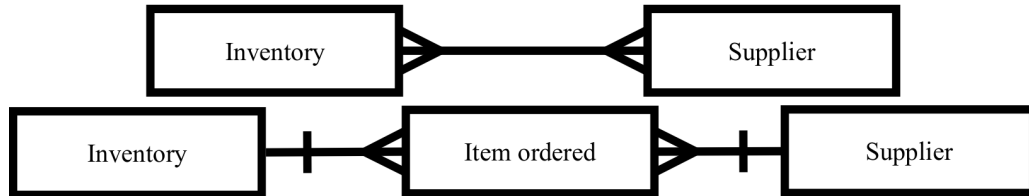


Figure 6: A many-to-many relationship can often be converted to two one-to-many relationships.

A means no occurrence of B. Cross-links and loops can exist, too. A recursive relationship is shown by drawing a semicircle from the entity back to itself.

For a variety of reasons, one-to-many relationships tend to be the most stable. Consequently, a primary objective of entity-relationship modeling is to convert one-to-one and many-to-many relationships into one-to-many relationships.

One-to-one relationships can often be merged. Generally, entities that share a one-to-one relationship are really the same entity and should be merged unless there is a good reason to keep them separate. Note that not all one-to-one relationships can be merged, however. For example, imagine a relationship between athletes and drug tests. There is one Drug test per Athlete and one Athlete per Drug test, so the relationship is clearly one-to-one. In this case, however, because merging the entities would probably violate security requirements (and possibly the law), there is a good logical reason to maintain separate entities.

Many-to-many relationships can cause maintenance problems. For example, Fig. 6 shows a many-to-many relationship between Inventory and Supplier. Each product in Inventory can have more than one Supplier, and each Supplier can carry more than one product. If a list of suppliers were stored in Inventory, adding or deleting a supplier might mean updating several Inventory occurrences. Likewise, listing products in Supplier could mean changing several Supplier occurrences if a single product were added or deleted.

One solution is to create a new entity that has a one-to-many relationship with both original entities. For example, imagine a new entity called Item ordered (Fig. 6). Given such a design, a given product in Inventory can appear on several active Items ordered, but each Item ordered is for one and only one product. Likewise, a given supplier can appear on several active Items ordered, but each Item ordered lists one and only one supplier. Note that a given Item ordered links a specific product in Inventory with a specific occurrence of Supplier. The many-to-many relationship has been converted to two one-to-many relationships.

### 2.1.3. ER diagrams

Assume a preliminary analysis of a retail sales application suggests four primary entities: customer, sales, inventory, and supplier. The Sales, Customer, and Inventory entities are related as follows. Customer initiates Sales. Sales are drawn from Inventory.

The first relationship is one-to-many (Fig. 7); a given Customer can have many Sales transactions, but a given Sale is associated with one and only one Customer. However, the second relationship is many-to-many because a given Sale can include several products from Inventory and a given product in Inventory can appear in many Sales.



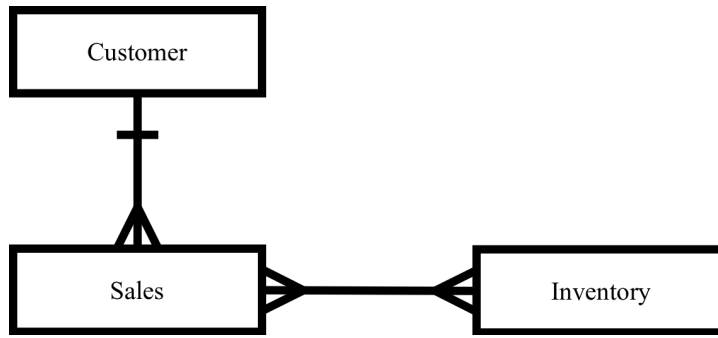


Figure 7: Customer, Sales and Inventory.

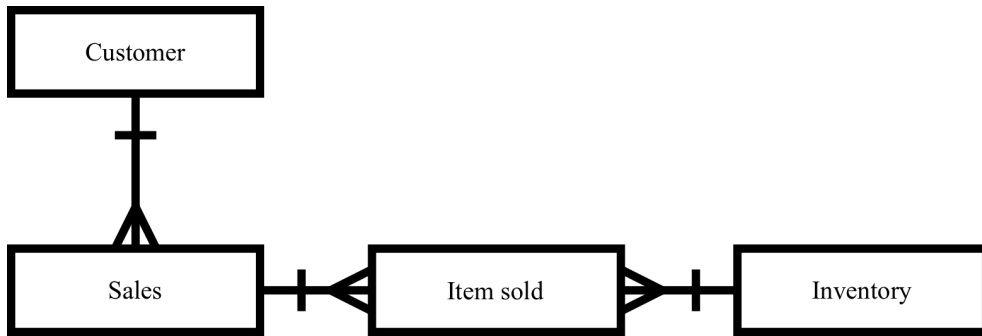


Figure 8: Resolving the many-to-many relationship calls for a new entity.

To resolve the many-to-many relationship, create a new entity, Item sold, that has a one-to-many relationship with both Sales and Inventory (Fig. 8). A given Sales transaction can list many Items sold, but a given Item sold is associated with one and only one Sales transaction. A given product in Inventory can appear in many Items sold, but a given Item sold lists one and only one product. (Think of an Item sold as one line in a list of products purchased on a sales invoice.)

There is one possible source of confusion about the Inventory entity that might need clarification. A specific 19-inch color television set is an example of a single occurrence of that entity, but Inventory might hold numerous virtually identical television sets. For inventory control purposes, tracking television sets (a class of occurrences) is probably good enough. However, the Customer purchases a specific television set (identified, perhaps, by concatenating the serial number to the stock number). Thus a given Item sold lists one and only one occurrence of Inventory.

The relationship between Inventory and Supplier (Fig. 9) is many-to-many because a given product can have many suppliers and a given supplier can supply many different products. Many-to-many relationships must be resolved, so add a new entity called Item ordered to the model, yielding two one-to-many relationships.

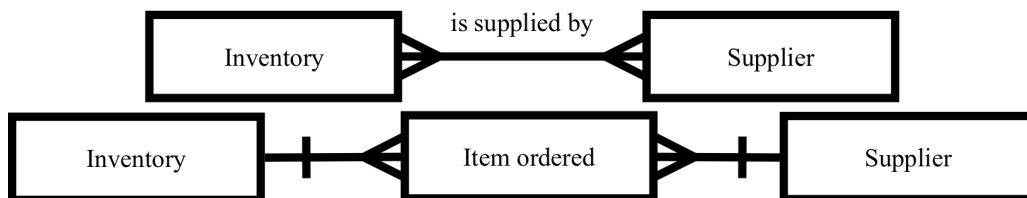


Figure 9: Creating a new entity called item ordered.

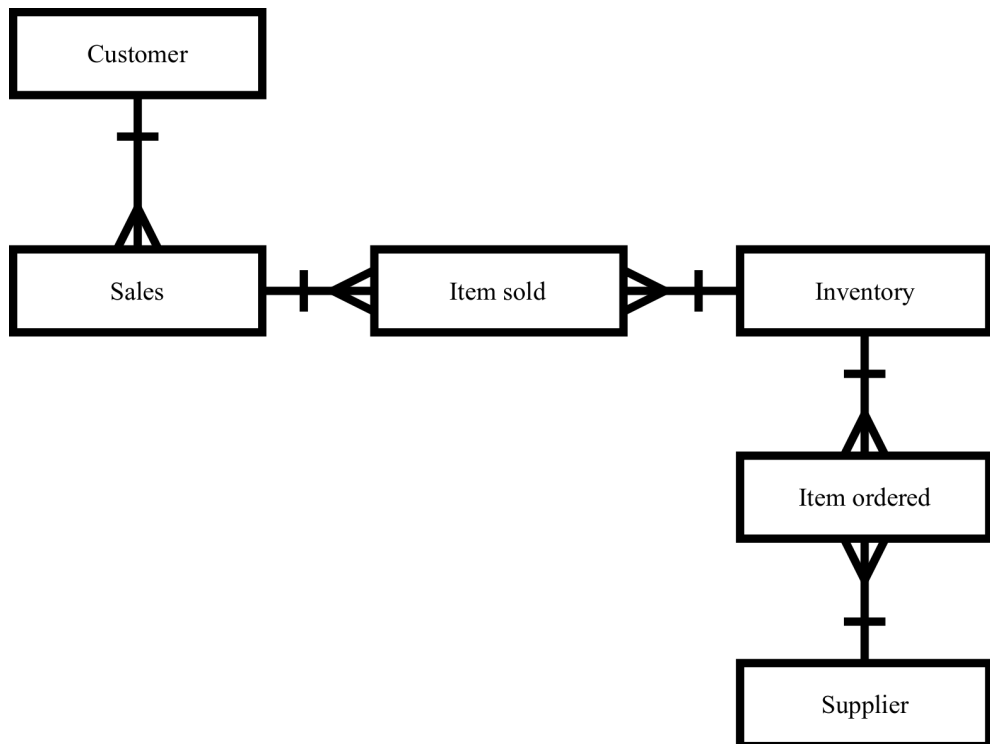


Figure 10: The finished entity-relationship model.

Title	Year	Length	Genre
Die Hard: With a Vengeance	1995	131	action
Pulp Fiction	1994	154	crime
King Kong	2005	187	adventure

Table 1: The relation Movies.

Finally, the Inventory entity is related to both Item sold and Item ordered, so combine the two partial diagrams to form a single entity-relationship model (Fig. 10).

## 2.2. Relational Model

The relational model gives us a single way to represent data: as a two-dimensional table called a relation. Table 1 is an example of a relation, which we shall call Movies. The rows each represent a movie, and the columns each represent a property of movies. We shall introduce the most important terminology regarding relations, and illustrate them with the Movies relation.

### 2.2.1. Attributes

The columns of a relation are named by attributes. In table 1 the attributes are title, year, length, and genre. Attributes appear at the tops of the columns. Usually, an attribute describes the meaning of entries in the column below. For instance, the column with attribute length holds the length, in minutes, of each movie.

### 2.2.2. Schemas

The name of a relation and the set of attributes for a relation is called the schema for that relation. We show the schema for the relation with the relation name followed by a parenthesized list of its attributes. Thus, the schema for relation Movies is

$$\text{Movies}(\text{title}, \text{year}, \text{length}, \text{genre}).$$

We shall generally follow the convention that relation names begin with a capital letter, and attribute names begin with a lower-case letter. The attributes in a relation schema are a set, not a list. However, in order to talk about relations we often must specify a "standard" order for the attributes. Thus, whenever we introduce a relation schema with a list of attributes, as above, we shall take this ordering to be the standard order whenever we display the relation or any of its rows.

In the relational model, a database consists of one or more relations. The set of schemas for the relations of a database is called a relational database schema, or just a database schema.

### 2.2.3. Tuples

The rows of a relation, other than the header row containing the attribute names, are called tuples. A tuple has one component for each attribute of the relation. For instance, the first of the three tuples in table 1 has the four components Die Hard: With a Vengeance, 1995, 131, action for attributes title, year, length, and genre, respectively. When we wish to write a tuple in isolation, not as part of a relation, we normally use commas to separate components, and we use parentheses to surround the tuple. For example,

$$(\text{Die Hard : With a Vengeance}, 1995, 131, \text{action})$$

is the first tuple of table 1. Notice that when a tuple appears in isolation, the attributes do not appear, so some indication of the relation to which the tuple belongs must be given. We shall always use the order in which the attributes were listed in the relation schema.

### 2.2.4. Domains

The relational model requires that each component of each tuple be atomic; that is, it must be of some elementary type such as integer or string. It is not permitted for a value to be a record structure, set, list, array, or any other type that reasonably can have its values broken into smaller components. It is further assumed that associated with each attribute of a relation is a domain, that is, a particular elementary type. The components of any tuple of the relation must have, in each component, a value that belongs to the domain of the corresponding column. For example, tuples of the Movies relation of table 1 must have a first component that is a string, second and third components that are integers, and a fourth component whose value is a string.

It is possible to include the domain, or data type, for each attribute in a relation schema. We shall do so by appending a colon and a type after attributes. For example, we could represent the schema for the Movies relation as:

$$\text{Movies}(\text{title} : \text{string}, \text{year} : \text{integer}, \text{length} : \text{integer}, \text{genre} : \text{string}).$$

### 2.2.5. Representations of a Relation

Relations are sets of tuples, not lists of tuples. Thus the order in which the tuples of a relation are presented is immaterial. For example, we can list the three tuples of table 1 in any of their six possible orders, and the relation is "the same" as in table 1. Moreover, we can reorder the attributes of the relation as we choose, without changing

Year	Genre	Title	Length
1995	action	Die Hard: With a Vengeance	131
1994	crime	Pulp Fiction	154
2005	adventure	King Kong	187

Table 2: Different representation of the relation Movies.

the relation. However, when we reorder the relation schema, we must be careful to remember that the attributes are column headers. Thus, when we change the order of the attributes, we also change the order of their columns. When the columns move, the components of tuples change their order as well. The result is that each tuple has its components permuted in the same way as the attributes are permuted.

For example, table 2 shows one of the many relations that could be obtained from relation shown at table 1 by permuting rows and columns. These two relations are considered as different presentations of the same relation.

### 2.2.6. Relation Instances

A relation about movies is not static; rather, relations change over time. We expect to insert tuples for new movies, as these appear. We also expect changes to existing tuples if we get revised or corrected information about a movie, and perhaps deletion of tuples for movies that are expelled from the database for some reason.

It is less common for the schema of a relation to change. However, there are situations where we might want to add or delete attributes. Schema changes, while possible in commercial database systems, can be very expensive, because each of perhaps millions of tuples needs to be rewritten to add or delete components. Also, if we add an attribute, it may be difficult or even impossible to generate appropriate values for the new component in the existing tuples.

We shall call a set of tuples for a given relation an instance of that relation. For example, the three tuples shown in table 1 form an instance of relation Movies. Presumably, the relation Movies has changed over time and will continue to change over time. For instance, in 2004, Movies did not contain the tuple for King Kong. However, a conventional database system maintains only one version of any relation: the set of tuples that are in the relation "now". This instance of the relation is called the current instance. Databases that maintain historical versions of data as it existed in past times are called temporal databases.

### 2.2.7. Keys of Relations

There are many constraints on relations that the relational model allows us to place on database schemas. The most fundamental type of constraints are the key constraints. A set of attributes forms a key for a relation if we do not allow two tuples in a relation instance to have the same values in all the attributes of the key.

For example, we can declare that the relation Movies has a key consisting of the two attributes title and year. That is, we do not believe there could ever be two movies that had both the same title and the same year. Notice that title by itself does not form a key, since sometimes "remakes" of a movie appear. For example, there are at least three movies named King Kong, each made in a different year.

We indicate the attribute or attributes that form a key for a relation by underlining the key attribute(s). For instance, the Movies relation could have its schema written as:

$$Movies(\underline{title}, \underline{year}, length, genre).$$

While we might be sure that title and year can serve as a key for Movies, many real-world databases use artificial keys, doubting that it is safe to make any assumption about the values of attributes outside their control. For example, companies generally assign employee ID's to all employees, and these ID's are carefully chosen to be unique numbers. One purpose of these ID's is to make sure that in the company database each employee can be

distinguished from all others, even if there are several employees with the same name. Thus, the employee-ID attribute can serve as a key for a relation about employees.

In US corporations, it is normal for every employee to have a Social-Security number. If the database has an attribute that is the Social-Security number, then this attribute can also serve as a key for employees. There is nothing wrong with there being several choices of key, as there would be for employees having both employee ID's and Social-Security numbers. These keys are then called equivalent keys, and one of them has to be chosen and used. The chosen key is called the primary key of a relation.

### 2.2.8. Functional Dependencies

First, we need to define the notion of r-value. If we have a set of attributes  $R = \{A_i | i = 1, \dots, k\}$ , an r-value, denoted by  $t[R]$  is a function that maps every attribute from  $R$  into a value from one record. Essentially, an r-value is a tuple, but it can also be only a part of a tuple too.

Functional dependency is a type of constraint that generalizes the notion of key constraint. It is defined on the set of relations and allows expression of inter relational constraints.

Expression of type  $f : X \rightarrow Y$ , where  $X$  and  $Y$  are sets of attributes, is called a functional dependency. It can be read that  $X$  functionally determines  $Y$ , and that  $Y$  functionally depends on  $X$ . It means that every element of the domain of the attribute  $X$  is mapped to element from domain of  $Y$ . Another words, if a value for the set of attributes  $X$  is given, then it uniquely determines a value for the set of attributes  $Y$ .

Formally, if a relation  $r$  over a set of attributes  $U$  is given, and  $X, Y \subseteq U$ , then a set of tuples of relation  $r$  satisfies a functional dependency  $f : X \rightarrow Y$  if for every two tuples  $u$  and  $v$  in  $r$  the following holds:

$$u[X] = v[X] \implies u[Y] = v[Y].$$

Functional dependencies are used to express constraints that could not be expressed by key constraints, especially inter-relation constraints.

Closure of a set of functional dependencies  $F$ , denoted by  $F^+$  is a set of all functional dependencies from  $F$  and those that can be derived from  $F$  using rules of inference. One set of rules of inference are Armstrong's axioms [1]. Let us assume that a set of functional dependencies  $F$  is defined over a set of attributes  $U$ , and that  $X, Y, Z$  and  $W$  are subsets of  $U$ . Then the Armstrong's axioms are the following

1. **Reflexivity:** if  $Y \subseteq X$ , then  $X \rightarrow Y$ ,
2. **Augmentation:** if  $X \rightarrow Y$  and  $Z \subseteq W$ , then  $XW \rightarrow YZ$ ,
3. **Pseudo transitivity:** if  $X \rightarrow Y$  and  $YW \rightarrow Z$ , then  $XW \rightarrow Z$ .

Now we can give an alternative definition of a key constraint. A set of attributes  $X \subseteq R$  is a key of a relation consisting of the set of attributes  $R$  and a set of functional dependencies  $F$  if and only if the following holds:

1.  $X \rightarrow Y \subseteq F^+$ ,
2.  $(\forall Y \subset X)(Y \rightarrow R \notin F^+)$ .

### 2.2.9. Referential integrity

The most important inter-relational constraint is a referential integrity. It is used to create links between tables. Informally, for referential integrity to hold, any field in a table that is declared a foreign key can contain only values from a parent table's primary key. For instance, deleting a record that contains a value referred to by a foreign key in another table would break referential integrity.

PId	LastName	FirstName	Address	City
1	Smith	John	5th Avenue 10	New York
2	Barnes	Kate	King's Avenue 23	London
3	Brown	Neil	Pitt Street 20	London

Table 3: Example database table.

For example, let us expand our movies database model with another table that represents movie directors. We can add a table that has three attributes - `personal_ID`, `first_name` and `last_name`. Personal ID is a primary key. Now we can make a link between table `Movies` and `Directors` by adding the attribute `personal_ID` under name `director` to the `Movies` table and demanding that this attribute has only values that already exist in the `Directors` table. This type of constraint is called referential integrity. Attribute `director` is called a foreign key. Our database could then be specified like this:

$$\begin{aligned} & \text{Movies}(\underline{\text{title}}, \underline{\text{year}}, \text{length}, \text{genre}, \text{director}), \\ & \text{Directors}(\underline{\text{personal\_ID}}, \text{first\_name}, \text{last\_name}), \end{aligned}$$

In addition, functional dependency  $\text{personal\_ID} \rightarrow \text{director}$  has to hold. Moreover, there is a separate notation for referential integrity constraint. In this case, we would write:

$$\text{Movies}[\text{director}] \subseteq \text{Directors}[\text{personal\_ID}].$$

It should be noted that a foreign key can contain more than one attribute if the primary key that it is drawn from contains more than one attribute.

Formal definition is a bit more complex. Let  $r_1$  and  $r_2$  be two relations containing a set of attributes  $R_1$  and  $R_2$  respectively. Let  $A_1, \dots, A_n \in R_1$  and  $B_1, \dots, B_n \in R_2$ , and let  $B_1, \dots, B_n$  be the key of relation  $r_2$ . Referential integrity  $r_1[A_1, \dots, A_n] \subseteq r_2[B_1, \dots, B_n]$  holds if and only if for every tuple  $t_1$  from  $r_1$  exists a tuple  $t_2$  from  $r_2$  so that  $t_1[A_k] = t_2[B_k]$  for every  $k = \{1, \dots, n\}$ .

### 3. SQL

SQL is a standard language for accessing and manipulating databases. SQL stands for Structured Query Language. It lets you access and manipulate databases. Although SQL is an ANSI (American National Standards Institute) standard, there are many different versions of the SQL language. SQL can:

- execute queries against a database,
- retrieve data from a database,
- insert, update and delete records in a database,
- create new databases and tables...

Below is an example of a table called "Persons". The table contains three records (one for each person) and five columns: `PId`, `LastName`, `FirstName`, `Address` and `City`.

Most of the actions we need to perform on a database are done with SQL statements. The following SQL statement will select all the records in the "Persons" table:

```
SELECT * FROM Persons
```

LastName	FirstName
Smith	John
Barnes	Kate
Brown	Neil

Table 4: Result-set.

SQL is not case sensitive. Some database systems require a semicolon at the end of each SQL statement. Semicolon is the standard way to separate each SQL statement in database systems that allow more than one SQL statement to be executed in the same call to the server. SQL can be divided into two parts: The Data Manipulation Language (DML) and the Data Definition Language (DDL).

Here is a list of query and update commands form the DML part of SQL:

- SELECT - extracts data from a database,
- UPDATE - updates data in a database,
- DELETE - deletes data from a database,
- INSERT INTO - inserts new data into a database.

The DDL part of SQL permits database tables to be created or deleted. It also define indexes (keys), specify links between tables, and impose constraints between tables. The most important DDL statements in SQL are:

- CREATE DATABASE - creates a new database,
- ALTER DATABASE - modifies a database,
- CREATE TABLE - creates a new table,
- ALTER TABLE - modifies a table,
- DROP TABLE - deletes a table,
- CREATE INDEX - creates an index (search key),
- DROP INDEX - deletes an index.

The SELECT statement is used to select data from a database. The result is stored in a result table, called the result-set. SQL SELECT statement has the following basic syntax:

```
SELECT column_name(s)
FROM table_name
```

Suppose we want to select the content of the columns named "LastName" and "FirstName" from the table 3. We use the following SELECT statement:

```
SELECT LastName , FirstName FROM Persons
```

The result-set is shown at table 4:

If we use:

```
SELECT * FROM Persons
```

City
New York
London

Table 5: Result-set.

PIId	LastName	FirstName	Address	City
2	Barnes	Kate	King's Avenue 23	London
3	Brown	Neil	Pitt Street 20	London

Table 6: Result-set.

we will select all the columns from the "Persons" table. The result-set will look just like the table 3.

In a table, some of the columns may contain duplicate values. This is not a problem, however, sometimes you will want to list only the different (distinct) values in a table. The DISTINCT keyword can be used to return only distinct (different) values. For example, if we want to select only the distinct values from the column named "City" from the table 3, we use the following SELECT statement:

```
SELECT DISTINCT City FROM Persons
```

The result-set is shown at table 5.

The WHERE clause is used to extract only those records that fulfill a specified criterion. It has the following syntax:

```
SELECT column_name(s)
FROM table_name
WHERE column_name operator value
```

If we want to select only the persons living in the city "London" from the table 3, we use the following SELECT statement:

```
SELECT * FROM Persons
WHERE City='London'
```

The result-set is shown at table 6.

SQL uses single quotes around text values. Most database systems will also accept double quotes. Although, numeric values should not be enclosed in quotes. For text values:

This is correct:

```
SELECT * FROM Persons WHERE FirstName='John'
```

This is wrong:

```
SELECT * FROM Persons WHERE FirstName=John
```

For numeric values: This is correct:

```
SELECT * FROM Persons WHERE Year=1965
```

This is wrong:

```
SELECT * FROM Persons WHERE Year='1965'
```

Table 7 shows operators that can be used with the WHERE clause.



Operator	Description
=	Equal
<>	Not equal
>	Greater than
<	Less than
>=	Greater than or equal
<=	Less than or equal
BETWEEN	Between an inclusive range
LIKE	Search for a pattern
IN	Belongs to a set

Table 7: WHERE operators.

PIId	LastName	FirstName	Address	City
1	Smith	John	5th Avenue 10	New York
3	Brown	Neil	Pitt Street 20	London

Table 8: Result-set.

The AND and OR operators are used to filter records based on more than one condition. The AND operator displays a record if both the first condition and the second condition is true. The OR operator displays a record if either the first condition or the second condition is true. If we wish to select only the persons with the first name equal to "John" AND the last name equal to "Smith", we use the following SELECT statement:

```
SELECT * FROM Persons
WHERE FirstName='John' AND LastName='Smith'
```

The result-set will contain only one record - (1, Smith, John, 5th Avenue 10, New York).

Similarly, if we want to select only the persons with the first name equal to "John" OR the first name equal to "Neil", we use the following SELECT statement:

```
SELECT * FROM Persons
WHERE FirstName='John' OR FirstName='Neil'
```

The result-set is shown at table 8.

One can also combine AND and OR and use parenthesis to form complex expressions. In addition, operator NOT can be used to form any kind of logic expression.

The ORDER BY keyword is used to sort the result-set by specified columns. It sorts the records in ascending order by default, but if we want to sort the records in a descending order, we can use the DESC keyword. If we wish to select all the persons from the table 3 and to sort the persons by their last name, we use the following SELECT statement:

```
SELECT * FROM Persons
ORDER BY LastName DESC
```

The result-set is shown at table 9.

The INSERT INTO statement is used to insert new records in a table. It is possible to write the INSERT INTO statement in two forms. The first form doesn't specify the column names where the data will be inserted, only their values:

```
INSERT INTO table_name
VALUES (value1 , value2 , value3 ,...)
```

The second form specifies both the column names and the values to be inserted:

PId	LastName	FirstName	Address	City
1	Smith	John	5th Avenue 10	New York
3	Brown	Neil	Pitt Street 20	London
2	Barnes	Kate	King's Avenue 23	London

Table 9: Result-set.

PId	LastName	FirstName	Address	City
1	Smith	John	5th Avenue 10	New York
2	Barnes	Kate	King's Avenue 23	London
3	Brown	Neil	Pitt Street 20	London
4	Jackson	Peter	Agnes Drive 17	Glasgow

Table 10: Example database table with added row.

```
INSERT INTO table_name (column1, column2, column3, ...)
VALUES (value1, value2, value3, ...)
```

For example, if we use the following SQL statement:

```
INSERT INTO Persons
VALUES (4, 'Jackson', 'Peter', 'Agnes Drive 17', 'Glasgow')
```

The "Persons" table will have another row, as shown at table 10:

The UPDATE statement is used to update existing records in a table. It has the following syntax:

```
UPDATE table_name
SET column1=value, column2=value2, ...
WHERE condition
```

We should first notice the WHERE clause in the UPDATE syntax. The WHERE clause specifies which record or records should be updated. If we omit the WHERE clause, all records will be updated! For example, if we wish to update the person Peter Jackson with alternate address, we can use the following SQL statement:

```
UPDATE Persons
SET Address='Albion Street 67'
WHERE LastName='Jackson' AND FirstName='Peter'
```

After the execution of this statement, content of the "Persons" table is shown at table 11.

The DELETE statement is used to delete rows in a table. It has the following syntax:

```
DELETE FROM table_name
WHERE condition
```

Similarly as with the UPDATE statement, the WHERE clause specifies which record or records should be deleted. Again, if it is omitted all records will be deleted! For example, consider the following DELETE statement:

PId	LastName	FirstName	Address	City
1	Smith	John	5th Avenue 10	New York
2	Barnes	Kate	King's Avenue 23	London
3	Brown	Neil	Pitt Street 20	London
4	Jackson	Peter	Albion Street 67	Glasgow

Table 11: Example database table after updates.

```
DELETE FROM Persons
WHERE LastName='Jackson' AND FirstName='Peter'
```

Clearly, after the execution, the fourth record will be deleted. So, the content of the “Persons” table will be the same as it was at the start, shown at table 3.

## 4. Normalization

Normalization is a design technique that is widely used as a guide in designing relational databases. It is essentially a two step process that puts data into tabular form by removing repeating groups and then removes duplicates from relational tables.

Normalization theory is based on the concepts of normal forms. A database is said to be in a particular normal form if it satisfied a certain set of constraints. There are currently at least eight normal forms that have been defined. In this section, we will cover the first three normal forms that were defined by the creator of the relational model, E. F. Codd [4]. Codd and Raymond Boyce defined the Boyce-Codd Normal Form (BCNF) in 1974 [5]. Higher normal forms like fourth [8], fifth [9] and domain/key normal form [10] were defined by other theorists in subsequent years. The most recent is the Sixth normal form (6NF) introduced by Chris Date, Hugh Darwen, and Nikos Lorentzos in 2002 [6].

### 4.1. Basic Concepts

The goal of normalization is to create a set of relational tables that are free of redundant data and that can be consistently and correctly modified. This means that all tables in a relational database should be in the third normal form (3NF). A relational table is in 3NF if and only if all non-key columns are:

1. mutually independent and
2. fully dependent on the primary key.

Mutual independence means that no non-key column is dependent upon any combination of the other columns. The first two normal forms are intermediate steps to achieve the goal of having all tables in 3NF. In order to better understand the 2NF and higher forms, it is necessary to understand the concepts of functional dependencies and lossless decomposition.

The concept of functional dependencies is the basis for the first three normal forms. As explained earlier, a column, Y, of the relational table R is said to be functionally dependent upon column X of R if and only if each value of X in R is associated with precisely one value of Y at any given time. X and Y may be composite. Saying that column Y is functionally dependent upon X is the same as saying the values of column X identify the values of column Y. If column X is a primary key, then all columns in the relational table R must be functionally dependent upon X.

Full functional dependence applies to tables with composite keys. Column Y in relational table R is fully functional on X of R if it is functionally dependent on X and not functionally dependent upon any subset of X. Full functional dependence means that when a primary key is composite, made of two or more columns, then the other columns must be identified by the entire key and not just some of the columns that make up the key.

Simply stated, normalization is the process of removing redundant data from relational tables by decomposing (splitting) a relational table into smaller tables by projection. The goal is to have only primary keys on the left hand side of a functional dependency. In order to be correct, decomposition must be lossless. That is, the new tables can be recombined by a natural join to recreate the original table without creating any spurious or redundant data.

Here is some sample data used to illustrate the process of normalization. A company obtains parts from a number of suppliers. Each supplier is located in one city. A city can have more than one supplier located there and each

s#	status	city	p#	qty
s1	20	London	p1	300
s1	20	London	p2	200
s1	20	London	p3	400
s1	20	London	p4	200
s1	20	London	p5	100
s1	20	London	p6	100
s2	10	Paris	p1	300
s2	10	Paris	p2	400
s3	10	Paris	p2	200
s4	20	London	p2	200
s4	20	London	p4	300
s4	20	London	p5	400

Table 12: Table in 1NF.

city has a status code associated with it. Each supplier may provide many parts. The company creates a simple relational table to store this information that can be expressed in relational notation as:

$$FIRST(s\#, status, city, p\#, qty),$$

where:

- s# is a supplier identification number,
- status is a status code assigned to city,
- city is a name of city where supplier is located,
- p# is a part number of part supplied and
- qty is a quantity of parts supplied to date.

In order to uniquely associate quantity supplied (qty) with part (p#) and supplier (s#), a composite primary key composed of s# and p# is used.

## 4.2. First Normal Form

A relational table, by definition, is in first normal form. All values of the columns are atomic. That is, they contain no repeating values. Table 12 shows the table FIRST in 1NF.

Although the table FIRST is in 1NF it contains redundant data. For example, information about the supplier's location and the location's status have to be repeated for every part supplied. Redundancy causes what are called update anomalies. Update anomalies are problems that arise when information is inserted, deleted, or updated. For example, the following anomalies could occur in FIRST:

1. INSERT. The fact that a certain supplier (s5) is located in a particular city (Athens) cannot be added until they supplied a part.
2. DELETE. If a row is deleted, then not only is the information about quantity and part lost but also information about the supplier.
3. UPDATE. If supplier s1 moved from London to New York, then six rows would have to be updated with this new information.

s#	status	city
s1	20	London
s2	10	Paris
s3	10	Paris
s4	20	London
s5	30	Athens

Table 13: SUPPLIER table.

### 4.3. Second Normal Form

The definition of second normal form states that only tables with composite primary keys can be in 1NF but not in 2NF.

A relational table is in second normal form 2NF if it is in 1NF and every non-key column is fully dependent upon the primary key. That is, every non-key column must be dependent upon the entire primary key. FIRST is in 1NF but not in 2NF because status and city are functionally dependent only on the column s# of the composite key (s#, p#). This can be illustrated by listing the functional dependencies in the table:

$$s\# \rightarrow (city, status),$$

$$city \rightarrow status,$$

$$(s\#, p\#) \rightarrow qty.$$

If we wanted to transform the table FIRST from 1NF to 2NF we could:

1. Identify any determinants other than the composite key, and the columns they determine.
2. Create and name a new table for each determinant and the unique columns it determines.
3. Move the determined columns from the original table to the new table.
4. The determinate becomes the primary key of the new table.
5. Delete the columns we just moved from the original table except for the determinate which will serve as a foreign key.

The original table may be renamed to maintain semantic meaning. To transform FIRST into 2NF we move the columns s#, status, and city to a new table called SUPPLIER. The column s# becomes the primary key of this new table. The results are shown at tables 13 and 14.

Tables in 2NF but not in 3NF still contain modification anomalies. In the example of SUPPLIER, they are:

1. INSERT. The fact that a particular city has a certain status (Rome has a status of 50) cannot be inserted until there is a supplier in the city.
2. DELETE. Deleting any row in SUPPLIER destroys the status information about the city as well as the association between supplier and city.

### 4.4. Third Normal Form

The third normal form requires that all columns in a database are dependent only upon the primary key. A more formal definition is:

s#	p#	qty
s1	p1	300
s1	p2	200
s1	p3	400
s1	p4	200
s1	p5	100
s1	p6	100
s2	p1	300
s2	p2	400
s3	p2	200
s4	p2	200
s4	p4	300
s4	p5	400

Table 14: PARTS table.

A database is in the third normal form (3NF) if it is already in 2NF and every non-key column is non transitively dependent upon its primary key. In other words, all non-key attributes are functionally dependent only upon the primary key.

Table PARTS is already in 3NF. The non-key column, qty, is fully dependent upon the primary key (s#, p#). SUPPLIER is in 2NF but not in 3NF because it contains a transitive dependency. A transitive dependency occurs when a non-key column that is a determinant of the primary key is the determinate of other columns. The concept of a transitive dependency can be illustrated by showing the functional dependencies in SUPPLIER:

$$\begin{aligned} \text{SUPPLIER.s\#} &\rightarrow \text{SUPPLIER.status}, \\ \text{SUPPLIER.s\#} &\rightarrow \text{SUPPLIER.city}, \\ \text{SUPPLIER.city} &\rightarrow \text{SUPPLIER.status}. \end{aligned}$$

Note that SUPPLIER.status is determined both by the primary key s# and the non-key column city. The process of transforming a table into 3NF is the following:

1. Identify any determinants, other than primary key, and the columns they determine.
2. Create and name a new table for each determinant and the unique columns it determines.
3. Move the determined columns from the original table to the new table.
4. The determinate becomes the primary key of the new table.
5. Delete the columns you just moved from the original table except for the determinate which will serve as a foreign key.

The original table may be renamed to maintain semantic meaning.

To transform SUPPLIER into 3NF, we create a new table called CITY\_STATUS and move the columns city and status into it. Status is deleted from the original table, city is left behind to serve as a foreign key to CITY\_STATUS, and the original table is renamed to SUPPLIER\_CITY to reflect its semantic meaning. The results of putting the original table into 3NF has created three tables. These can be represented as:

$$\begin{aligned} &PARTS(s\#, p\#, qty) \\ &SUPPLIER\_CITY(s\#, city) \\ &CITY\_STATUS(city, status) \\ &PARTS[s\#] \subseteq SUPPLIER\_CITY[s\#] \\ &SUPPLIER\_CITY[s\#] \subseteq CITY\_STATUS[city]. \end{aligned}$$

court	start_time	end_time	rate_type
1	09:30	10:30	SAVER
1	11:00	12:00	SAVER
1	14:00	15:30	STANDARD
2	10:00	11:30	PREMIUM-B
2	11:30	13:30	PREMIUM-B
2	15:00	16:30	PREMIUM-A

Table 15: Today's court bookings table.

The advantages to having relational tables in 3NF is that it eliminates redundant data which in turn saves space and reduces manipulation anomalies. For example, the improvements to our sample database are:

1. INSERT. Facts about the status of a city, Rome has a status of 50, can be added even though there is not supplier in that city. Likewise, facts about new suppliers can be added even though they have not yet supplied parts.
2. DELETE. Information about parts supplied can be deleted without destroying information about a supplier or a city.
3. UPDATE. Changing the location of a supplier or the status of a city requires modifying only one row.

#### 4.5. Boyce-Codd Normal Form

The Boyce-Codd normal form is a slightly stronger version of the third normal form. A table is in Boyce-Codd normal form if and only if for every one of its nontrivial dependencies  $X \rightarrow Y$ ,  $X$  is a superkey - that is,  $X$  is either a candidate key or a superset thereof. BCNF was developed in 1974 by Raymond Boyce and Edgar Codd to address certain types of anomaly not dealt with by 3NF as originally defined [5].

Only in rare cases does a 3NF table not meet the requirements of BCNF. A 3NF table which does not have multiple overlapping candidate keys is guaranteed to be in BCNF [16]. Depending on what its functional dependencies are, a 3NF table with two or more overlapping candidate keys may or may not be in BCNF. An example of a 3NF table that does not meet BCNF is shown in table 15.

Each row in the table represents a court booking at a tennis club that has one hard court (Court 1) and one grass court (Court 2). A booking is defined by its court and the period for which the court is reserved. Additionally, each booking has a rate type associated with it. There are four distinct rate types:

- SAVER, for Court 1 bookings made by members,
- STANDARD, for Court 1 bookings made by non-members,
- PREMIUM-A, for Court 2 bookings made by members and
- PREMIUM-B, for Court 2 bookings made by non-members.

The table's candidate keys are:  $\{\text{court, start\_time}\}$ ,  $\{\text{court, end\_time}\}$ ,  $\{\text{rate\_type, start\_time}\}$ ,  $\{\text{rate\_type, end\_time}\}$ .

Recall that 2NF prohibits partial functional dependencies of non-prime attributes on candidate keys, and that 3NF prohibits transitive functional dependencies of non-prime attributes on candidate keys. In the Today's Court Bookings table, there are no non-prime attributes: that is, all attributes belong to candidate keys. Therefore the table adheres to both 2NF and 3NF. The table does not adhere to BCNF. This is because of the dependency  $\text{rate\_type} \rightarrow \text{court}$ , in which the determining attribute (rate type) is neither a candidate key nor a superset of a candidate key.

## 4.6. Normalization algorithms

There are two basic methods for normalization - decomposition and synthesis. There are many variations to these methods, but the ideas are the same. Decomposition method is based on progressive decomposition of database schema consisting of all attributes in a database in accordance to constraint given by functional dependencies. Decomposition progresses until a database in desired normal form is obtained. The best normal form that is guaranteed by the algorithm is the Boyce-Codd normal form.

The synthesis method, on the other hand, is based on a completely different approach. It is realized by using functional dependencies only. The input is again, a set of all attributes of a database, together with a set of functional dependencies. The output is a database at least in third normal form. Tables are synthesized from functional dependencies. The basic idea is based on reduction and elimination of redundant functional dependencies from the initial set.

Detailed description of these algorithms is way beyond the scope of this text. That information can be found in, for instance [13, 2]. It is important to note that the decomposition method guarantees better normal form than the synthesis method. It guarantees that the resulting database will be in the Boyce-Codd normal form, while the synthesis algorithm takes us only to the third normal form, in the worst case. This is an advantage of the decomposition method. On the other hand, the decomposition method does not guarantee the conservation of initial set of functional dependencies. It is possible that some nontrivial functional dependencies are lost in the process. Important data about the database structure can be lost with them. On the other hand, the synthesis method guarantees the conservation of the initial set of functional dependencies. There is another important advantage of the synthesis method. Its complexity is polynomial, while the complexity of the decomposition method is exponential. This gives the synthesis method decisive advantage in the case of large databases.

The fact that the method of synthesis does not necessarily gives a database in BCNF has small significance for practical usage. In practice, databases in 3NF and not in BCNF are rare. On the other hand, conservation of initial set of functional dependencies is important because it guarantees that the resulting database content will be in accordance to constraints in the real world expressed by functional dependencies.

Normalization is an important step in database design methodology. However, manual use of normalization algorithms can be conducted only with small and simple databases. Automatization of these methods is the only solution. Since the method of synthesis has polynomial complexity, in difference to exponential complexity of the method of decomposition, it is generally a better choice.

## References

- [1] William Ward Armstrong. Dependency structures of data base relationships. In *IFIP Congress*, pages 580–583, 1974.
- [2] Philip A. Bernstein. Synthesizing third normal form relations from functional dependencies. *ACM Trans. Database Syst.*, 1:277–298, December 1976.
- [3] Edgar Frank Codd. A relational model of data for large shared data banks. *Communications of the ACM*, 13(6):377–387, 1970.
- [4] Edgar Frank Codd. Further normalization of the data base relational model. *IBM Research Report, San Jose, California*, RJ909, 1971.
- [5] Edgar Frank Codd. Recent investigations into relational data base systems. Technical Report RJ1385, IBM, 4 1974.
- [6] Chris Date, Hugh Darwen, and Nikos Lorentzos. *Temporal Data and the Relational Model*. Morgan Kaufmann Publishers Inc., San Francisco, CA, USA, 2002.
- [7] Christopher J. Date. *An Introduction to Database Systems, Eighth Edition*. Addison Wesley, July 2003.



- [8] Ronald Fagin. Multivalued dependencies and a new normal form for relational databases. *ACM Trans. Database Syst.*, 2:262–278, September 1977.
- [9] Ronald Fagin. Normal forms and relational database operators. In *Proceedings of the 1979 ACM SIGMOD international conference on Management of data, SIGMOD '79*, pages 153–160, New York, NY, USA, 1979. ACM.
- [10] Ronald Fagin. A normal form for relational databases that is based on domains and keys. *ACM Trans. Database Syst.*, 6:387–415, September 1981.
- [11] Hector Garcia-Molina, Jeffrey D. Ullman, and Jennifer Widom. *Database Systems: The Complete Book*. Prentice Hall Press, Upper Saddle River, NJ, USA, 2 edition, 2008.
- [12] Miloš Racković, Srdjan Škrbić, and Jovana Vidaković. *Introduction to Databases*. Faculty of Science, Novi Sad, Serbia, 2007.
- [13] K. V. S. V. N. Raju and Arun K. Majumdar. Fuzzy functional dependencies and lossless join decomposition of fuzzy relational database systems. *ACM Trans. Database Syst.*, 13:129–166, June 1988.
- [14] Peter Pin shan Chen. The entity-relationship model: Toward a unified view of data. *ACM Transactions on Database Systems*, 1:9–36, 1976.
- [15] A. Silberschatz, H. Korth, and S. Sudarshan. *Database Systems Concepts*. McGraw-Hill, Inc., New York, NY, USA, 5 edition, 2006.
- [16] Millist Vincent and Bala Srinivasan. A note on relation schemes which are in 3nf but not in bcnf. *Inf. Process. Lett.*, 48:281–283, December 1993.